

# Comparison of Centrality and Power-Flow-Based Contingency Indices

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#### Goals

- Attempt to validate graph-theory-based approaches to power system contingency ranking using limited system information (due to the difficulty inherent to acquiring complete system information, a coordinated system attack is more likely to be planned from limited information).
- Develop an approach to identify higher-order contingency scenarios that have a statistically significant likelihood of resulting in a maximally adverse impact given incomplete system information.
- Assist with the development of a test-bed from which attack scenarios can be simulated in real-time, and the resulting data utilized by a vulnerability-related application tool.

### **Fundamental Questions/Challenges**

- We seek to answer the question of whether or not high-impact contingencies can be identified without extensive operational knowledge of a power system. Challenge: conventional contingency screening methods utilize power-flow-based screening techniques requiring knowledge of system branch and shunt impedances, bus MVA injection, and bus voltage magnitudes to check for contingencies that would result in a voltage or branch flow violation.
- We wish to pursue a solution to the question of how to utilize graph theory in the development of an N-X contingency ranking scheme.
  Challenge: graph-theory-based centrality techniques have not been developed to assess the collective importance of a given group of buses or branches.

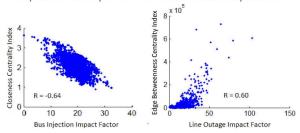
#### Research Plan

- Estimate system impedances and topology via physical observation of the power grid or readily available standards information and maps.
- Calculate degree, eigenvector, closeness, and vertex betweenness centralities for each bus in a power system.
- Calculate edge betweenness centrality for each branch in a power system.
- Use conventional DC power flow contingency screening techniques to calculate generation shift factors (GSF) and line outage distribution factors (LODF).
- Create DC power-flow-based line outage and bus injection sensitivity indices based on the DC power flow GSF and LODF factors.
- Correlate centrality indices with DC power-flow-based index to determine which centrality techniques have some statistically significant relationship to an existing contingency screening technique.
- Using the Wilcoxon signed rank test, determine the agreement in highly ranked contingencies between DC power flow and centrality-based indices.
- Draw conclusions concerning which centrality technique is the best candidate for developing a topology-based algorithm to identify higher-order contingencies.

#### Research Results

 Closeness centrality correlates well with a DC power-flow-based bus injection impact factor index, and edge betweenness centrality correlates well with a DC power-flow-based line outage impact factor.

Comparison of Centrality and DC Power Flow Based Vulnerability Measures



 A comparison of the top ten ranked line contingencies for a DC powerflow-based measure and edge betweenness centrality concluded these two ranking systems identified statistically similar top-ranked contingencies across multiple test systems.

Wilcoxon Signed Rank Test for Top 10 Vulnerabilities: Edge Betweenness Centrality Matched to DC Power-Flow-Based Line Outage Index.

Test System	N	Estimated	Lower	Upper	Achieved
		Median	Bound	Bound	Confidence
IEEE-14	10	3.0	-1.5	7.0	94.7%
IEEE-30	10	5.0	-2.0	11.5	94.7%
IEEE-57	10	6.0	-1.5	10.0	94.7%
Polish-2383	10	5.0	-1.5	58	94.7%

## **Broader Impact**

- Research would result in significant findings for power grid vulnerability analysis using incomplete system information. If graph theory can be reliably utilized to select targets for a coordinated attack on the power system, an attacker can assess the vulnerability of a power system without obtaining confidential power system operational data.
- A graph-theory-based approach to contingency ranking would utilize mathematical tools more familiar to computer scientists, potentially leading to enhanced participation of computer scientists in smart grid research.
- The developed test-bed can be utilized by multiple institutions for further research studies.

# **Interaction with Other Projects**

- Work is inspired by the publication "Electrical Centrality Measures for Electric Power Grid Vulnerability Analysis" from Wang (UI Urbana-Champaign), Scaglione (UC Davis), and Thomas (Cornell).
- Results will serve as an application tool for coordinating cyber attack scenarios simulated with the test-bed being developed using funding from NSF, DOE, and industry partners.

#### **Future Efforts**

- Develop a centrality-based N-X contingency ranking algorithm that has a statistically significant relationship with a conventional N-X AC powerflow-based contingency ranking index.
- Investigate whether or not graph-theory-based network flow algorithms are adequate candidates for developing a contingency ranking index.



